Two-view geometry



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16-385 Computer Vision Spring 2021, Lecture 11

Overview of today's lecture

- Triangulation.
- Epipolar geometry.
- Essential matrix.
- Fundamental matrix.
- 8-point algorithm.

Slide credits

Many of these slides were adapted from:

- Kris Kitani (16-385, Spring 2017).
- Srinivasa Narasimhan (16-720, Fall 2017).















Given a set of (noisy) matched points $\{m{x}_i,m{x}_i'\}$

and camera matrices

 \mathbf{P},\mathbf{P}'

Estimate the 3D point

Х



known known

Can we compute **X** from a single correspondence **x**?

$\mathbf{x} = \mathbf{P} \mathbf{X}$

This is a similarity relation because it involves homogeneous coordinates



coordinate)

Same ray direction but differs by a scale factor

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \alpha \begin{bmatrix} p_1 & p_2 & p_3 & p_4 \\ p_5 & p_6 & p_7 & p_8 \\ p_9 & p_{10} & p_{11} & p_{12} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

How do we solve for unknowns in a similarity relation?

Linear algebra reminder: cross product

Vector (cross) product

takes two vectors and returns a vector perpendicular to both



$$m{u} imes m{b} = \left[egin{array}{c} a_2 b_3 - a_3 b_2 \ a_3 b_1 - a_1 b_3 \ a_1 b_2 - a_2 b_1 \end{array}
ight]$$

cross product of two vectors in the same direction is zero vector ${m a} imes {m a} = 0$

remember this!!!

Linear algebra reminder: cross product

Cross product

$$m{a} imes m{b} = \left[egin{array}{c} a_2 b_3 - a_3 b_2 \ a_3 b_1 - a_1 b_3 \ a_1 b_2 - a_2 b_1 \end{array}
ight]$$

Can also be written as a matrix multiplication

$$m{a} imes m{b} = [m{a}]_{ imes} m{b} = egin{bmatrix} 0 & -a_3 & a_2 \ a_3 & 0 & -a_1 \ -a_2 & a_1 & 0 \end{bmatrix} egin{bmatrix} b_1 \ b_2 \ b_3 \end{bmatrix}$$

Skew symmetric

Compare with: dot product



dot product of two orthogonal vectors is (scalar) zero

Back to triangulation

$\mathbf{x} = \alpha \mathbf{P} \mathbf{X}$

Same direction but differs by a scale factor

How can we rewrite this using vector products?

$\mathbf{x} = \alpha \mathbf{P} \mathbf{X}$

Same direction but differs by a scale factor

$\mathbf{x} \times \mathbf{P} \boldsymbol{X} = \mathbf{0}$

Cross product of two vectors of same direction is zero (this equality removes the scale factor)

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \alpha \begin{bmatrix} p_1 & p_2 & p_3 & p_4 \\ p_5 & p_6 & p_7 & p_8 \\ p_9 & p_{10} & p_{11} & p_{12} \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$
$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \alpha \begin{bmatrix} - & p_1^\top & - \\ - & p_2^\top & - \\ - & p_3^\top & - \end{bmatrix} \begin{bmatrix} 1 \\ X \\ 1 \end{bmatrix}$$
$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \alpha \begin{bmatrix} p_1^\top X \\ p_2^\top X \\ p_3^\top X \end{bmatrix}$$
$$\begin{bmatrix} p_1^\top X \\ p_3^\top X \end{bmatrix} = \alpha \begin{bmatrix} p_1^\top X \\ p_2^\top X \\ p_3^\top X \end{bmatrix} = \alpha \begin{bmatrix} p_1^\top X \\ p_2^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \end{bmatrix} = \alpha \begin{bmatrix} p_1^\top X \\ p_2^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \\ p_3^\top X \end{bmatrix} = \begin{bmatrix} p_1^\top X \\ p_3^\top X \end{bmatrix} =$$

Do the same after first expanding out the camera matrix and points

$$\begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \times \begin{bmatrix} \boldsymbol{p}_1^\top \boldsymbol{X} \\ \boldsymbol{p}_2^\top \boldsymbol{X} \\ \boldsymbol{p}_3^\top \boldsymbol{X} \end{bmatrix} = \begin{bmatrix} y \boldsymbol{p}_3^\top \boldsymbol{X} - \boldsymbol{p}_2^\top \boldsymbol{X} \\ \boldsymbol{p}_1^\top \boldsymbol{X} - x \boldsymbol{p}_3^\top \boldsymbol{X} \\ x \boldsymbol{p}_2^\top \boldsymbol{X} - y \boldsymbol{p}_1^\top \boldsymbol{X} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

Using the fact that the cross product should be zero

$\mathbf{x} imes \mathbf{P} \boldsymbol{X}$:	= ()
$\left[egin{array}{c} y oldsymbol{p}_3^ op oldsymbol{X} - oldsymbol{p}_2^ op oldsymbol{X} \ oldsymbol{p}_1^ op oldsymbol{X} - x oldsymbol{p}_3^ op oldsymbol{X} \ x oldsymbol{p}_2^ op oldsymbol{X} - y oldsymbol{p}_1^ op oldsymbol{X} \end{array} ight]$		$\left[\begin{array}{c} 0\\ 0\\ 0\\ 0 \end{array}\right]$

Third line is a linear combination of the first and second lines. (x times the first line plus y times the second line)

One 2D to 3D point correspondence give you equations

Using the fact that the cross product should be zero

$\mathbf{x} imes \mathbf{P} oldsymbol{X}$:	= ()
$\left[egin{array}{c} y oldsymbol{p}_3^ op oldsymbol{X} - oldsymbol{p}_2^ op oldsymbol{X} \ oldsymbol{p}_1^ op oldsymbol{X} - x oldsymbol{p}_3^ op oldsymbol{X} \ x oldsymbol{p}_2^ op oldsymbol{X} - y oldsymbol{p}_1^ op oldsymbol{X} \end{array} ight]$	=	$\left[\begin{array}{c} 0\\ 0\\ 0\\ 0\end{array}\right]$

Third line is a linear combination of the first and second lines. (x times the first line plus y times the second line)

One 2D to 3D point correspondence give you 2 equations

$$\left[\begin{array}{c} y \boldsymbol{p}_3^\top \boldsymbol{X} - \boldsymbol{p}_2^\top \boldsymbol{X} \\ \boldsymbol{p}_1^\top \boldsymbol{X} - x \boldsymbol{p}_3^\top \boldsymbol{X} \end{array}\right] = \left[\begin{array}{c} 0 \\ 0 \end{array}\right]$$

Remove third row, and rearrange as system on unknowns

$$egin{array}{c} y oldsymbol{p}_3^{ op} - oldsymbol{p}_2^{ op} \ oldsymbol{p}_1^{ op} - x oldsymbol{p}_3^{ op} \end{array} iggree egin{array}{c} oldsymbol{X} = \left[egin{array}{c} 0 \ 0 \end{array}
ight] oldsymbol{X} = \left[egin{array}{c} 0 \ 0 \end{array}
ight]$$

 $\mathbf{A}_i \boldsymbol{X} = \boldsymbol{0}$

Now we can make a system of linear equations (two lines for each 2D point correspondence) Concatenate the 2D points from both images

Two rows from camera one

Two rows from camera two



sanity check! dimensions?

 $\mathbf{A} \boldsymbol{X} = \boldsymbol{0}$

How do we solve homogeneous linear system?

Concatenate the 2D points from both images



$\mathbf{A}X = \mathbf{0}$

How do we solve homogeneous linear system?

SVD!

Epipolar geometry







Epipolar geometry



Epipolar geometry












Quiz



Quiz



Quiz





Another way to construct the epipolar plane, this time given $oldsymbol{x}$

Epipolar constraint







Where is the epipole in this image?



Where is the epipole in this image?

It's not always in the image

Parallel cameras





Where is the epipole?

Parallel cameras







epipole at infinity

The epipolar constraint is an important concept for stereo vision

Task: Match point in left image to point in right image



Left image

Right image

How would you do it?

Epipolar constraint



The epipolar constraint is an important concept for stereo vision

Task: Match point in left image to point in right image



Left image

Right image

Want to avoid search over entire image Epipolar constraint reduces search to a single line The epipolar constraint is an important concept for stereo vision

Task: Match point in left image to point in right image



Left image

Right image

Want to avoid search over entire image Epipolar constraint reduces search to a single line

How do you compute the epipolar line?

The essential matrix

Recall:Epipolar constraint



Given a point in one image, multiplying by the **essential matrix** will tell us the **epipolar line** in the second view.



Motivation

The Essential Matrix is a 3 x 3 matrix that encodes **epipolar geometry**

Given a point in one image, multiplying by the **essential matrix** will tell us the **epipolar line** in the second image.

Epipolar Line





If the point $oldsymbol{x}$ is on the epipolar line $oldsymbol{l}$ then

$$x^{\top}l = ?$$

Epipolar Line





If the point $oldsymbol{x}$ is on the epipolar line $oldsymbol{l}$ then

 $\boldsymbol{x}^{ op} \boldsymbol{l} = 0$





Essential Matrix vs Homography

What's the difference between the essential matrix and a homography?

Essential Matrix vs Homography

What's the difference between the essential matrix and a homography?

They are both 3 x 3 matrices but ...

 $l' = \mathbf{E} \boldsymbol{x}$

Essential matrix maps a **point** to a **line**

x' = Hx

Homography maps a **point** to a **point**

Where does the essential matrix come from?

















putting it together



putting it together

rigid motion coplanarity

$$m{x}' = \mathbf{R}(m{x} - m{t}) \qquad (m{x} - m{t})^{ op}(m{t} imes m{x}) = 0$$

ymmetric $(m{x}'^{ op} \mathbf{R})(m{t} imes m{x}) = 0$
present cross $(m{x}'^{ op} \mathbf{R})([m{t}_{ imes}]m{x}) = 0$

use skew-symmetric matrix to represent cross product

putting it together


putting it together



putting it together



Longuet-Higgins equation

 $x'^{ op}\mathbf{E}x=0$

(2D points expressed in <u>camera</u> coordinate system)

Longuet-Higgins equation

$$\boldsymbol{x}^{\prime \top} \mathbf{E} \boldsymbol{x} = 0$$

Epipolar lines
$$egin{array}{ccc} m{x}^ op m{l} = 0 & m{x}'^ op m{l}' = 0 \ m{l}' = m{E}m{x} & m{l} = m{E}^Tm{x}' \end{array}$$

(2D points expressed in <u>camera</u> coordinate system)

Longuet-Higgins equation

$$\boldsymbol{x}^{\prime op} \mathbf{E} \boldsymbol{x} = 0$$

Epipolar lines
$$egin{array}{ccc} m{x}^{ op}m{l}=0 & m{x}'^{ op}m{l}'=0 \ m{l}=m{E}^Tm{x}' & m{l}=m{E}^Tm{x}' \end{array}$$

Epipoles
$$e'^ op \mathbf{E} = \mathbf{0}$$
 $\mathbf{E} e = \mathbf{0}$

(2D points expressed in <u>camera</u> coordinate system)

Given a point in one image, multiplying by the **essential matrix** will tell us the **epipolar line** in the second view.



2D points expressed in camera coordinate system (i.e., intrinsic matrices are identities)

How do you generalize to non-identity intrinsic matrices?

The fundamental matrix

The fundamental matrix is a generalization of the essential matrix, where the assumption of **Identity matrices** is removed

 $\hat{\boldsymbol{x}}^{\prime \top} \mathbf{E} \hat{\boldsymbol{x}} = 0$

The essential matrix operates on image points expressed in **2D coordinates expressed in the camera coordinate system**

 $\hat{\boldsymbol{x}'} = \mathbf{K}'^{-1} \boldsymbol{x}'$

 $\hat{x} = \mathbf{K}^{-1} x$

camera point image point

 $\hat{\boldsymbol{x}}^{\prime \top} \mathbf{E} \hat{\boldsymbol{x}} = 0$

The essential matrix operates on image points expressed in **2D coordinates expressed in the camera coordinate system**

$$\hat{x'} = \mathbf{K}'^{-1} x'$$



Writing out the epipolar constraint in terms of image coordinates

$$\mathbf{K}^{\prime - \top} \mathbf{E} \mathbf{K}^{-1} \mathbf{x} = 0$$
$$\mathbf{x}^{\prime \top} (\mathbf{K}^{\prime - \top} \mathbf{E} \mathbf{K}^{-1}) \mathbf{x} = 0$$
$$\mathbf{x}^{\prime \top} \mathbf{F} \mathbf{x} = \mathbf{0}$$

Same equation works in image coordinates!

 $\mathbf{x}^{\prime \top} \mathbf{F} \mathbf{x} = 0$

it maps pixels to epipolar lines

Longuet-Higgins equation

$$\boldsymbol{x}^{\prime op} \mathbf{E} \boldsymbol{x} = 0$$

Epipolar lines
$$egin{array}{ccc} m{x}^{ op}m{l}=0 & m{x}'^{ op}m{l}'=0 \ m{l}=m{E}m{x} & m{l}=m{E}^Tm{x}' \end{array}$$

Epipoles
$$e'^ op \mathbf{E} = \mathbf{0}$$
 $\mathbf{E} e = \mathbf{0}$

(points in **image** coordinates)

Breaking down the fundamental matrix

$\mathbf{F} = \mathbf{K}'^{-\top} \mathbf{E} \mathbf{K}^{-1}$ $\mathbf{F} = \mathbf{K}'^{-\top} [\mathbf{t}_{\times}] \mathbf{R} \mathbf{K}^{-1}$

Depends on both intrinsic and extrinsic parameters

Breaking down the fundamental matrix

$\mathbf{F} = \mathbf{K}'^{-\top} \mathbf{E} \mathbf{K}^{-1}$ $\mathbf{F} = \mathbf{K}'^{-\top} [\mathbf{t}_{\times}] \mathbf{R} \mathbf{K}^{-1}$

Depends on both intrinsic and extrinsic parameters

How would you solve for F?

$$oldsymbol{x}_m^{\prime op} \mathbf{F} oldsymbol{x}_m = 0$$

The 8-point algorithm

Assume you have *M* matched *image* points

$$\{\boldsymbol{x}_m, \boldsymbol{x}_m'\}$$
 $m = 1, \dots, M$

Each correspondence should satisfy

$$oldsymbol{x}_m^{\prime op} \mathbf{F} oldsymbol{x}_m = 0$$

How would you solve for the 3 x 3 **F** matrix?

Assume you have *M* matched *image* points

$$\{\boldsymbol{x}_m, \boldsymbol{x}_m'\}$$
 $m = 1, \dots, M$

Each correspondence should satisfy

$$oldsymbol{x}_m^{\prime op} \mathbf{F} oldsymbol{x}_m = 0$$

How would you solve for the 3 x 3 **F** matrix?

SVD!

Assume you have *M* matched *image* points

$$\{\boldsymbol{x}_m, \boldsymbol{x}_m'\}$$
 $m = 1, \dots, M$

Each correspondence should satisfy

 $\boldsymbol{x}_m^{\prime op} \mathbf{F} \boldsymbol{x}_m = 0$

How would you solve for the 3 x 3 **F** matrix?

Set up a homogeneous linear system with 9 unknowns

$$oldsymbol{x}_m^{\prime op} \mathbf{F} oldsymbol{x}_m = 0$$
 $\left[egin{array}{cccc} x_m^{\prime op} & y_m^{\prime op} & 1 \end{array}
ight] \left[egin{array}{ccccc} f_1 & f_2 & f_3 \ f_4 & f_5 & f_6 \ f_7 & f_8 & f_9 \end{array}
ight] \left[egin{array}{ccccc} x_m \ y_m \ 1 \end{array}
ight] = 0$

How many equation do you get from one correspondence?

$$\begin{bmatrix} x'_{m} & y'_{m} & 1 \end{bmatrix} \begin{bmatrix} f_{1} & f_{2} & f_{3} \\ f_{4} & f_{5} & f_{6} \\ f_{7} & f_{8} & f_{9} \end{bmatrix} \begin{bmatrix} x_{m} \\ y_{m} \\ 1 \end{bmatrix} = 0$$

ONE correspondence gives you ONE equation

$$x_m x'_m f_1 + x_m y'_m f_2 + x_m f_3 + y_m x'_m f_4 + y_m y'_m f_5 + y_m f_6 + x'_m f_7 + y'_m f_8 + f_9 = 0$$

$$\begin{bmatrix} x'_{m} & y'_{m} & 1 \end{bmatrix} \begin{bmatrix} f_{1} & f_{2} & f_{3} \\ f_{4} & f_{5} & f_{6} \\ f_{7} & f_{8} & f_{9} \end{bmatrix} \begin{bmatrix} x_{m} \\ y_{m} \\ 1 \end{bmatrix} = 0$$

Set up a homogeneous linear system with 9 unknowns

How many equations do you need?

Each point pair (according to epipolar constraint) contributes only one <u>scalar</u> equation

$$\boldsymbol{x}_m^{\prime op} \mathbf{F} \boldsymbol{x}_m = 0$$

Note: This is different from the Homography estimation where each point pair contributes 2 equations.

We need at least 8 points

Hence, the 8 point algorithm!

How do you solve a homogeneous linear system?

$\mathbf{A} \mathbf{X} = \mathbf{0}$

How do you solve a homogeneous linear system?

$\mathbf{A} \mathbf{X} = \mathbf{0}$

Total Least Squares minimize $\|\mathbf{A}\mathbf{x}\|^2$

subject to $\| \boldsymbol{x} \|^2 = 1$

How do you solve a homogeneous linear system?

$\mathbf{A} \mathbf{X} = \mathbf{0}$

Total Least Squares minimize $\|\mathbf{A}\mathbf{x}\|^2$ subject to $\|\mathbf{x}\|^2 = 1$

SVD!

0. (Normalize points)

- 1. Construct the M x 9 matrix **A**
- 2. Find the SVD of $\boldsymbol{\mathsf{A}}$
- 3. Entries of ${\bf F}$ are the elements of column of

V corresponding to the least singular value

- 4. (Enforce rank 2 constraint on F)
- 5. (Un-normalize F)

0. (Normalize points)

- 1. Construct the M x 9 matrix **A**
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How do we do this?

0. (Normalize points)

- 1. Construct the M x 9 matrix **A**
- 2. Find the SVD of A
- 3. Entries of ${\bf F}$ are the elements of column of

V corresponding to the least singular value

How do we do this?

4. (Enforce rank 2 constraint on F)

5. (Un-normalize F)

Enforcing rank constraints

Problem: Given a matrix F, find the matrix F' of rank k that is closest to F,

$$\min_{F'} ||F - F'||^2$$
$$\operatorname{rank}(F') = k$$

Solution: Compute the singular value decomposition of F,

$$F = U\Sigma V^T$$

Form a matrix Σ ' by replacing all but the k largest singular values in Σ with 0.

Then the problem solution is the matrix **F'** formed as,

$$F' = U\Sigma' V^T$$

0. (Normalize points)

- 1. Construct the M x 9 matrix **A**
- 2. Find the SVD of $\boldsymbol{\mathsf{A}}$
- 3. Entries of ${\bf F}$ are the elements of column of

V corresponding to the least singular value

- 4. (Enforce rank 2 constraint on F)
- 5. (Un-normalize F)

Example



epipolar lines



$$\mathbf{F} = \begin{bmatrix} -0.00310695 & -0.0025646 & 2.96584 \\ -0.028094 & -0.00771621 & 56.3813 \\ 13.1905 & -29.2007 & -9999.79 \end{bmatrix}$$

$$\mathbf{x} = \begin{bmatrix} 343.53\\ 221.70\\ 1.0 \end{bmatrix}$$
$$\mathbf{l}' = \mathbf{F}\mathbf{x}$$
$$= \begin{bmatrix} 0.0295\\ 0.9996\\ -265.1531 \end{bmatrix}$$

$${}^{\prime} = \mathbf{F} oldsymbol{x} \ = \left[egin{array}{c} 0.0295 \ 0.9996 \ -265.1531 \end{array}
ight]$$


Where is the epipole?



How would you compute it?



$\mathbf{F} \boldsymbol{e} = \boldsymbol{0}$

The epipole is in the right null space of ${\bf F}$

How would you solve for the epipole?



$\mathbf{F} \boldsymbol{e} = \boldsymbol{0}$

The epipole is in the right null space of ${\bf F}$

How would you solve for the epipole?

