

# Programming Assignment 2

## Augmented Reality with Planar Homographies

Due Date: Wed February 21, 2024 23:59

In this assignment, you will be implementing an AR application step by step using planar homographies. Before we step into the implementation, we will walk you through the theory of planar homographies. In the programming section, you will first learn to find point correspondences between two images and use these to estimate the homography between them. Using this homography you will then warp images and finally implement your own AR application.

### 1 Instructions

1. **Integrity and collaboration:** Students are encouraged to work in groups but each student must submit their own work. If you work as a group, include the names of your collaborators in your write up. Code should **NOT** be shared or copied. Please **DO NOT** use external code unless permitted. Plagiarism is strongly prohibited and may lead to failure of this course.
2. **Start early!** This is a much bigger assignment than assignment 1.
3. **Questions:** If you have any questions, please look at Piazza first. Other students may have encountered the same problem, and it may be solved already. If not, post your question on the discussion board. Teaching staff will respond as soon as possible.
4. **Write-up:** Your write-up should mainly consist of three parts, your answers to theory questions, resulting images of each step, and the discussions for experiments. Please note that we **DO NOT** accept handwritten scans for your write-up in this assignment. Please type your answers to theory questions and discussions for experiments electronically.
5. Please stick to the function prototypes mentioned in the handout. This makes verifying code easier for the TAs.
6. **Submission:** Handing in your assignments involves two separate submissions via Gradescope: (a) submit your **full** solution (which includes the write-up) in a single zip file, and (b) submit your write-up as a pdf file. The submission time will be the later of the two timestamps associated with these submissions. For example, if you submit your full solution before the deadline and submit your write-up 1 day late, your assignment will be considered 1 day late.

### (a) Submitting your Full solution

Each assignment includes a short Bash script, `zip.sh`. Although assignments can be zipped manually, we recommend using the script to zip your solution as follows: use a terminal to open the directory containing the script and run it. An autograder on Gradescope will check whether you formatted your files correctly (i.e., includes required files in the layout described below); **assignments that do not pass the autograder will be deducted 10 points**. Your zip file, `<AndrewID>.zip`, should then be uploaded to Gradescope. Note that the file size limit for Gradescope is 100 MBs.

The zip file is composed of your write-up, your Python implementations (including any helper functions), and your implementations & results for extra credit (optional). Please make sure to remove the `data/` folder, `loadVid.py`, `helper.py`, and any other temporary files you've generated.

Your final upload **MUST** have the files arranged and named in this layout:

- `<AndrewId>.zip`
  - `<AndrewId>.pdf`
  - `python/`
    - \* `ar.py`
    - \* `briefRotTest.py`
    - \* `HarryPotterize.py`
    - \* `matchPics.py`
    - \* `planarH.py`
    - \* `yourHelperFunctions.py` (*optional*)
  - `result/`
    - \* `ar.avi`
  - `ec/` (*optional for extra credit*)
    - \* `ar_ec.py`
    - \* `panorama.py`
    - \* the images required for generating the results.

### (b) Submitting your Write-up

In addition to including your write-up in the full solution, you are also required to create a separate submission on Gradescope for your write-up only. Once submitted, **double check that the write-up can be viewed from within Gradescope and that you submitted the correct file!!**

7. **File paths:** Please make sure that any file paths that you use are relative and not absolute. Not `cv2.imread('/name/Documents/subdirectory/hw2/data/xyz.jpg')` but `cv2.imread('../data/xyz.jpg')`.

## 2 Homographies

### Planar Homographies as a Warp

Recall that a planar homography is an warp operation (which is a mapping from pixel coordinates from one camera frame to another) that makes a fundamental assumption of the points lying on a plane in the real world. Under this particular assumption, pixel coordinates in one view of the points on the plane can be *directly* mapped to pixel coordinates in another camera view of the same points, through a homography  $\mathbf{H}$ :

$$\mathbf{x}_1 \equiv \mathbf{H}\mathbf{x}_2 \quad (1)$$

The  $\equiv$  symbol stands for *identical to*. The points  $\mathbf{x}_1$  and  $\mathbf{x}_2$  are in *homogeneous coordinates*, which means they have an additional dimension. If  $\mathbf{x}_1$  is a 3D vector  $[x_i \ y_i \ z_i]^T$ , it represents the 2D point  $[\frac{x_i}{z_i} \ \frac{y_i}{z_i}]^T$  (called *inhomogeneous* or *heterogeneous coordinates*). This additional dimension is a mathematical convenience to represent transformations (like translation, rotation, scaling, etc) in a concise matrix form. The  $\equiv$  means that the equation is correct to a scaling factor.

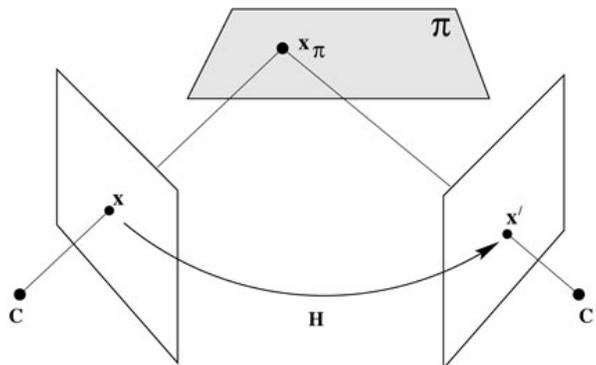


Figure 1: A homography  $\mathbf{H}$  links all points  $\mathbf{x}_\pi$  lying in plane  $\pi$  between two camera views  $\mathbf{x}$  and  $\mathbf{x}'$  in cameras  $C$  and  $C'$  respectively such that  $\mathbf{x}' = \mathbf{H}\mathbf{x}$ .

[From Hartley and Zisserman]

### The Direct Linear Transform

A very common problem in projective geometry is often of the form  $\mathbf{x} \equiv \mathbf{A}\mathbf{y}$ , where  $\mathbf{x}$  and  $\mathbf{y}$  are known vectors, and  $\mathbf{A}$  is a matrix which contains unknowns to be solved. Given matching points in two images, our homography relationship clearly is an instance of such a problem. Note that the equality holds only *up to scale* (which means that the set of equations are of the form  $\mathbf{x} = \lambda\mathbf{H}\mathbf{x}'$ ), which is why we cannot use an ordinary least squares solution such as what you may have used in the past to solve simultaneous equations. A standard approach to solve these kinds of problems is called the Direct Linear Transform, where we rewrite

the equation as proper homogeneous equations which are then solved in the standard least squares sense. Since this process involves disentangling the structure of the  $\mathbf{H}$  matrix, it's a *transform* of the problem into a set of *linear* equations, thus giving it its name.

**Q2.1 Correspondences** (10 points)

Let  $\mathbf{x}_1$  be a set of points in an image and  $\mathbf{x}_2$  be the set of corresponding points in an image taken by another camera. Suppose there exists a homography  $\mathbf{H}$  such that:

$$\mathbf{x}_1^i \equiv \mathbf{H}\mathbf{x}_2^i \quad (i \in \{1 \dots N\})$$

where  $\mathbf{x}_1^i = [x_1^i \ y_1^i \ 1]^T$  are in homogeneous coordinates,  $\mathbf{x}_1^i \in \mathbf{x}_1$  and  $\mathbf{H}$  is a  $3 \times 3$  matrix. For each point pair, this relation can be rewritten as

$$\mathbf{A}_i \mathbf{h} = 0$$

where  $\mathbf{h}$  is a column vector reshaped from  $\mathbf{H}$ , and  $\mathbf{A}_i$  is a matrix with elements derived from the points  $\mathbf{x}_1^i$  and  $\mathbf{x}_2^i$ . This can help calculate  $\mathbf{H}$  from the given point correspondences.

1. How many degrees of freedom does  $\mathbf{h}$  have? (2 points)
2. How many point pairs are required to solve  $\mathbf{h}$ ? (2 points)
3. Derive  $\mathbf{A}_i$ . (3 points)
4. When solving  $\mathbf{A}\mathbf{h} = 0$ , in essence you're trying to find the  $\mathbf{h}$  that exists in the null space of  $\mathbf{A}$ . What that means is that there would be some non-trivial solution for  $\mathbf{h}$  such that that product  $\mathbf{A}\mathbf{h}$  turns out to be 0. What will be a trivial solution for  $\mathbf{h}$ ? What is the rank of matrix  $\mathbf{A}$ ? (3 points)

**Q2.2 Fun with Homogeneous Coordinates** (15 points)

The equation for a conic in the plane using heterogeneous coordinates  $(x, y)$  is

$$ax^2 + bxy + cy^2 + dx + ey + f = 0. \quad (2)$$

1. Suppose you are given a set of heterogeneous points  $\tilde{\mathbf{x}}_i = (x_i, y_i)$ ,  $i = 1, \dots, N$ . Derive an expression for the (homogeneous) least squares estimate of the conic  $\mathbf{c} = (a, b, c, d, e, f)$  passing through those points. Your expression may take the form of a null vector or eigenvector of a matrix; if so, you must provide expressions for the matrix elements. (5 points)
2. In general, what is the minimum value of  $N$  that allows a unique solution for  $\mathbf{c}$ ? (3 points)
3. "Homogenize" Eq. 2 by making the substitutions  $x \rightarrow x_1/x_3$ ,  $y \rightarrow x_2/x_3$ , and show that in terms of homogeneous coordinates ( $\mathbf{x} = (x_1, x_2, x_3)$ ) the conic can be expressed in matrix form,

$$\mathbf{x}^T \mathbf{C} \mathbf{x} = 0,$$

with a symmetric matrix  $\mathbf{C}$ . (4 points)

4. Suppose we apply a projective transformation to our points:  $\mathbf{x}'_i = \mathbf{H}\mathbf{x}_i$ . The transformed points  $\mathbf{x}'_i$  will lie on a transformed conic represented by a new symmetric matrix  $\mathbf{C}'$ . Write an equation that specifies the relationship between  $\mathbf{C}'$  and  $\mathbf{C}$ , in terms of the homography  $\mathbf{H}$ . (3 points)

## Using Matrix Decompositions to calculate the homography

A homography  $\mathbf{H}$  transforms one set of points (in homogeneous coordinates) to another set of points. In this project, we will obtain the corresponding point coordinates using feature matches and will then need to calculate the homography. You have already derived that  $\mathbf{A}\mathbf{x} = \mathbf{0}$  in Question 2. In this section, we will look at how to solve such equations using two approaches, either of which can be used in the subsequent assignment questions.

## Eigenvalue Decomposition

One way to solve  $\mathbf{A}\mathbf{x} = \mathbf{0}$  is to calculate the eigenvalues and eigenvectors of  $\mathbf{A}$ . The eigenvector corresponding to  $\mathbf{0}$  is the answer for this. Consider this example:

$$\mathbf{A} = \begin{bmatrix} 3 & 6 & -8 \\ 0 & 0 & 6 \\ 0 & 0 & 2 \end{bmatrix}$$

Using the `numpy.linalg` function `eig`, we get the following eigenvalues and eigenvectors:

$$V = \begin{bmatrix} 1.0000 & -0.8944 & -0.9535 \\ 0 & 0.4472 & 0.2860 \\ 0 & 0 & 0.0953 \end{bmatrix}$$

$$D = \begin{bmatrix} 3 & 0 & 2 \end{bmatrix}$$

Here, the columns of  $\mathbf{V}$  are the eigenvectors and each corresponding element in  $\mathbf{D}$  it's eigenvalue. We notice that there is an eigenvalue of 0. The eigenvector corresponding to this is the solution for the equation  $\mathbf{A}\mathbf{x} = \mathbf{0}$ .

$$\mathbf{A}\mathbf{x} = \begin{bmatrix} 3 & 6 & -8 \\ 0 & 0 & 6 \\ 0 & 0 & 2 \end{bmatrix} \begin{bmatrix} -0.8944 \\ 0.4472 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

## Singular Value Decomposition

The Singular Value Decomposition (SVD) of a matrix  $\mathbf{A}$  is expressed as:

$$\mathbf{A} = U\Sigma V^T$$

Here,  $U$  is a matrix of column vectors called the “left singular vectors”. Similarly,  $V$  is called the “right singular vectors”. The matrix  $\Sigma$  is a diagonal matrix. Each diagonal element  $\sigma_i$  is called the “singular value” and these are sorted in order of magnitude. In our case, it is a  $9 \times 9$  matrix.

- If  $\sigma_9 = 0$ , the system is *exactly-determined*, a homography exists and all points fit exactly.
- If  $\sigma_9 \geq 0$ , the system is *over-determined*. A homography exists but not all points fit exactly (they fit in the least-squares error sense). This value represents the goodness of fit.
- Usually, you will have at least four correspondences. If not, the system is *under-determined*. We will not deal with those here.

The columns of  $U$  are eigenvectors of  $\mathbf{A}\mathbf{A}^T$ . The columns of  $V$  are the eigenvectors of  $\mathbf{A}^T\mathbf{A}$ . We can use this fact to solve for  $\mathbf{h}$  in the equation  $\mathbf{A}\mathbf{h} = \mathbf{0}$ . Using this knowledge, let us reformulate our problem of solving  $\mathbf{A}\mathbf{x} = \mathbf{0}$ . We want to minimize the error in solution in the least-squares sense. Ideally, the product  $\mathbf{A}\mathbf{h}$  should be 0. Thus the sum-squared error can be written as:

$$\begin{aligned} f(\mathbf{h}) &= \frac{1}{2}(\mathbf{A}\mathbf{h} - \mathbf{0})^T(\mathbf{A}\mathbf{h} - \mathbf{0}) \\ &= \frac{1}{2}(\mathbf{A}\mathbf{h})^T(\mathbf{A}\mathbf{h}) \\ &= \frac{1}{2}\mathbf{h}^T\mathbf{A}^T\mathbf{A}\mathbf{h} \end{aligned}$$

Minimizing this error with respect to  $\mathbf{h}$ , we get:

$$\begin{aligned} \frac{d}{d\mathbf{h}}f &= 0 \\ \implies \frac{1}{2}(\mathbf{A}^T\mathbf{A} + (\mathbf{A}^T\mathbf{A})^T)\mathbf{h} &= 0 \\ \mathbf{A}^T\mathbf{A}\mathbf{h} &= 0 \end{aligned}$$

This implies that the value of  $\mathbf{h}$  equals the eigenvector corresponding to the zero eigenvalue (or closest to zero in case of noise). Thus, we choose the smallest eigenvalue of  $\mathbf{A}^T\mathbf{A}$ , which is  $\sigma_9$  in  $\Sigma$  and the least-squares solution to  $\mathbf{A}\mathbf{h} = \mathbf{0}$  is the the corresponding eigenvector (in column 9 of the matrix  $\mathbf{V}$ ).

## 3 Computing Planar Homographies

### Feature Detection and Matching

Before finding the homography between an image pair, we need to find corresponding point pairs between two images. But how do we get these points? One way is to select them

manually, which is tedious and inefficient. The CV way is to find interest points in the image pair and automatically match them. In the interest of being able to do cool stuff, we will not reimplement a feature detector or descriptor here, but use python modules. The purpose of an interest point detector (e.g. Harris, SIFT, SURF, etc.) is to find particular salient points in the images around which we extract feature descriptors (e.g. MOPS, etc.). These descriptors try to summarize the content of the image around the feature points in as succinct yet descriptive manner possible (there is often a trade-off between representational and computational complexity for many computer vision tasks; you can have a very high dimensional feature descriptor that would ensure that you get good matches, but computing it could be prohibitively expensive). Matching, then, is a task of trying to find a descriptor in the list of descriptors obtained after computing them on a new image that best matches the current descriptor. This could be something as simple as the Euclidean distance between the two descriptors, or something more complicated, depending on how the descriptor is composed. For the purpose of this exercise, we shall use the widely used FAST detector in concert with the BRIEF descriptor.

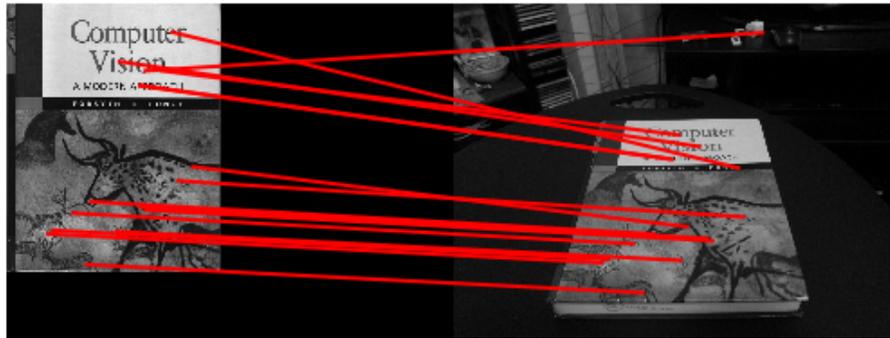


Figure 2: A few matched FAST feature points with the BRIEF descriptor.

**Q3.1 FAST Detector** (5 points)

How is the FAST detector different from the Harris corner detector that you've seen in the lectures? (You will probably need to look up the FAST detector online.) Can you comment on its computational performance vis-à-vis the Harris corner detector?

**Q3.2 BRIEF Descriptor** (5 points)

How is the BRIEF descriptor different from the filterbanks you've seen in the lectures? Could you use any one of those filter banks as a descriptor?

**Q3.3 Matching Methods** (5 points)

The BRIEF descriptor belongs to a category called binary descriptors. In such descriptors the image region corresponding to the detected feature point is represented as a binary string of 1s and 0s. A commonly used metric used for such descriptors is called the *Hamming distance*. Please search online to learn about Hamming distance

and *Nearest Neighbor*, and describe how they can be used to match interest points with BRIEF descriptors. What benefits does the Hamming distance have over a more conventional Euclidean distance measure in our setting?

### Q3.4 Feature Matching

(10 points)

Please implement a function:

```
matches, locs1, locs2 = matchPics(I1, I2)
```

where `I1` and `I2` are the images you want to match. `locs1` and `locs2` are  $N_1 \times 2$  and  $N_2 \times 2$  matrices, respectively, containing the  $x$  and  $y$  coordinates of the feature points. `matches` is a  $p \times 2$  matrix where the first column is indices into features in `I1`, and similarly the second column contains indices related to `I2`. Use the provided helper function `corner_detection` to compute the features, then build descriptors using the provided helper function `computeBrief`, and finally compare them using the provided helper function `briefMatch`.

Use the provided helper function `plotMatches` to visualize your matched points and include the resulting image in your write-up. An example is shown in Fig. 2.

The number of matches between the two images varies based on the parameter `sigma` used in `corner_detection`, and also on the value `ratio` in `briefMatch`. You should vary these to get the best results. The example shown in Fig. 2 is with `sigma = 0.15` and `ratio = 0.65`.

We provide you with the following helper functions:

```
locs = corner_detection(img, sigma)
desc, locs = computeBrief(img, locs)
matches = briefMatch(desc1, desc2)
plotMatches(im1, im2, matches, locs1, locs2)
```

`locs` is an  $N \times 2$  matrix in which each row represents the location  $(x, y)$  of a feature point. Please note that the number of valid output feature points can be less than the number of input feature points. `desc` is the corresponding matrix of BRIEF descriptors for the interest points.

**In your write-up:** As stated above, use the provided helper function `plotMatches` to visualize your matched points and include the resulting image in your write-up.

### Q3.5 BRIEF and Rotations

(10 points)

Let's investigate how BRIEF works with rotations. Write a script `briefRotTest.py` that:

- Takes the `cv_cover.jpg` and matches it to itself rotated [*Hint: use `scipy.ndimage.rotate`*] in increments of 10 degrees.

- Stores a histogram of the count of matches for each orientation.
- Plots the histogram using `matplotlib.pyplot.bar`

**In your write-up:** Include visualizations of the feature matching results at three different orientations. Explain why you think the BRIEF descriptor behaves this way.

## Homography Computation

### Q3.6 Computing the Homography

(15 points)

Write a function `computeH` that estimates the planar homography from a set of matched point pairs.

$$\mathbf{H2to1} = \text{computeH}(\mathbf{x1}, \mathbf{x2})$$

$\mathbf{x1}$  and  $\mathbf{x2}$  are  $N \times 2$  matrices containing the coordinates  $(x, y)$  of point pairs between the two images.  $\mathbf{H2to1}$  should be a  $3 \times 3$  matrix for the best homography from image 2 to image 1 in the least-square sense. The `numpy.linalg` functions `eig` or `svd` will be useful to get the eigenvectors (see Section 2 of this handout for details).

## Homography Normalization

Normalization improves numerical stability of the solution and you should always normalize your coordinate data. Normalization has two steps:

1. Translate the mean of the points to the origin.
2. Scale the points so that the largest distance to the origin is  $\sqrt{2}$ .

This is a linear transformation and can be written as follows:

$$\tilde{\mathbf{x}}_1 = \mathbf{T}_1 \mathbf{x}_1$$

$$\tilde{\mathbf{x}}_2 = \mathbf{T}_2 \mathbf{x}_2$$

where  $\tilde{\mathbf{x}}_1$  and  $\tilde{\mathbf{x}}_2$  are the normalized homogeneous coordinates of  $\mathbf{x}_1$  and  $\mathbf{x}_2$ .  $\mathbf{T}_1$  and  $\mathbf{T}_2$  are  $3 \times 3$  matrices.

The homography  $\mathbf{H}$  from  $\tilde{\mathbf{x}}_2$  to  $\tilde{\mathbf{x}}_1$  computed by `computeH` satisfies:

$$\tilde{\mathbf{x}}_1 = \mathbf{H} \tilde{\mathbf{x}}_2$$

By substituting  $\tilde{\mathbf{x}}_1$  and  $\tilde{\mathbf{x}}_2$  with  $\mathbf{T}_1 \mathbf{x}_1$  and  $\mathbf{T}_2 \mathbf{x}_2$ , we have:

$$\mathbf{T}_1 \mathbf{x}_1 = \mathbf{H} \mathbf{T}_2 \mathbf{x}_2$$

$$\mathbf{x}_1 = \mathbf{T}_1^{-1} \mathbf{H} \mathbf{T}_2 \mathbf{x}_2$$

### Q3.7 Homography with normalization

(10 points)

Implement the function `computeH_norm`:

$$\mathbf{H}_{2\text{to}1} = \text{computeH\_norm}(\mathbf{x}_1, \mathbf{x}_2)$$

This function should normalize the coordinates in  $\mathbf{x}_1$  and  $\mathbf{x}_2$  and call `computeH( $\mathbf{x}_1, \mathbf{x}_2$ )` as described above.

## RANSAC

The RANSAC algorithm can generally fit any model to noisy data. You will implement it for (planar) homographies between images. Remember that 4 point-pairs are required at a minimum to compute a homography.

### Q3.8 Implement RANSAC for computing a homography

(25 points)

Write a function:

$$\text{bestH}_{2\text{to}1}, \text{inliers} = \text{computeH\_ransac}(\mathbf{x}_1, \mathbf{x}_2)$$

where `bestH2to1` should be the homography  $\mathbf{H}$  with most inliers found during RANSAC.  $\mathbf{H}$  will be a homography such that if  $\mathbf{x}_2$  is a point in  $\mathbf{x}_2$  and  $\mathbf{x}_1$  is a corresponding point in  $\mathbf{x}_1$ , then  $\mathbf{x}_1 \equiv \mathbf{H}\mathbf{x}_2$ .  $\mathbf{x}_1$  and  $\mathbf{x}_2$  are  $N \times 2$  matrices containing the matched points. `inliers` is a vector of length  $N$  with a 1 at those matches that are part of the consensus set, and 0 elsewhere. Use `computeH_norm` to compute the homography.

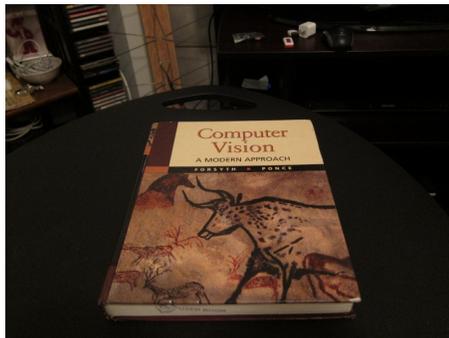


Figure 3: Text book

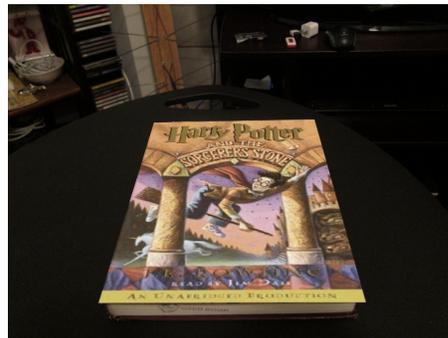


Figure 4: HarryPotterized Text book

## Automated Homography Estimation and Warping

### Q3.9 Putting it together

(10 points)

Write a script `HarryPotterize.py` that

1. Reads `cv_cover.jpg`, `cv_desk.png`, and `hp_cover.jpg`.
2. Computes a homography automatically using `MatchPics` and `computeH_ransac`.
3. Uses the computed homography to warp `hp_cover.jpg` to the dimensions of the `cv_desk.png` image using the `skimage` function `skimage.transform.warp` or OpenCV function `cv2.warpPerspective`.
4. At this point you should notice that although the image is being warped to the correct location, it is not filling up the same space as the book. Why do you think this is happening? How would you modify `hp_cover.jpg` to fix this issue?
5. Implement the function:

```
composite_img = compositeH( H2to1, template, img )
```

to now compose this warped image with the desk image as in in Figure 4

**In your write-up:** Show us your final image, `composite_img`, generated by your script `HarryPotterize.py`. Also, discuss the questions raised in item #4.

## 4 Creating your Augmented Reality application

### Q4.1 Incorporating video

(20 points)

Now with the code you have, you're able to create you own Augmented Reality application. What you're going to do is HarryPoterize the video `ar_source.mov` onto the video `book.mov`. More specifically, you're going to track the computer vision text book in each frame of `book.mov`, and overlay each frame of `ar_source.mov` onto the book in `book.mov`. Please write a script `ar.py` to implement this AR application and save your result video as `ar.avi` in the `result/` directory. You may use the function `loadVid` that we provide to load the videos. You'll be given full credits if you can put the video together correctly. See Figure 5 for an example frame of what the final video should look like.

Note that the book and the videos we have provided have very different aspect ratios (the ratio of the image width to the image height). You must crop each frame to fit onto the book cover. You should crop each frame such that only its central region is used in the final output. See Figure 6 for an example.

Also, the video `book.mov` only has translation of objects. If you want to account for rotation of objects, scaling, etc, you would have to pick a better feature point representation (like ORB).



Figure 5: Rendering video on a moving target



Figure 6: Crop out the yellow regions of each frame to match the aspect ratio of the book

## 5 Extra Credit

### Q5.1x: Create a Simple Panorama

(10 points)

Take two pictures with your own camera, separated by a pure rotation as best as possible, and then construct a panorama with `panorama.py`. Be sure that objects in the images are far enough away so that there are no parallax effects. You can use python module `cpselect` to select matching points on each image or some automatic method. Submit the original images, the final panorama, and the script `panorama.py` that loads the images and assembles a panorama. We have provided two images for you to get started (`data/pano_left.png` and `data/pano_right.png`). Please use your own images when submitting this assignment.

**In your write-up:** Include your original images and the panorama result image. See Figure 8-10 below for example.



Figure 7: Original Image 1 (left)



Figure 8: Original Image 2 (right)

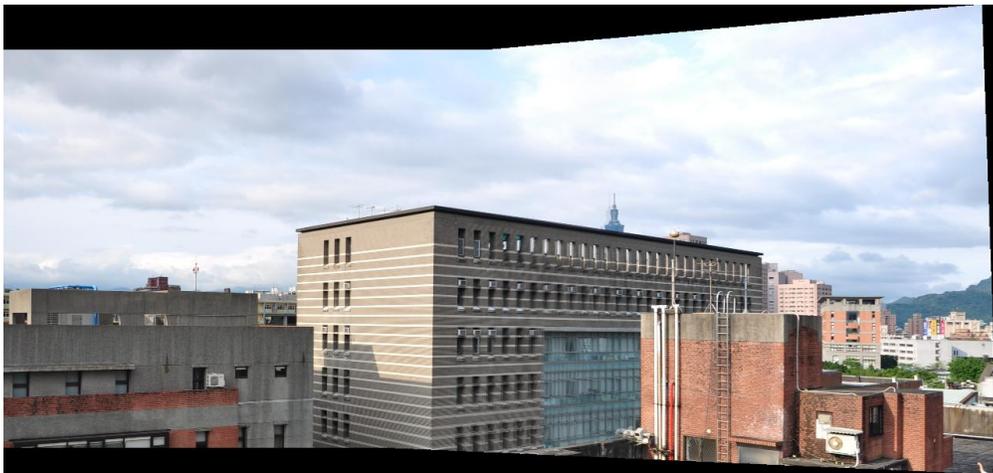


Figure 9: Panorama